Available online at scholarcommons.usf.edu/ijis

International Journal of Speleology

Official Journal of Union Internationale de Spéléologie

The relationship between carbon dioxide concentration and visitor numbers in the homothermic zone of the Balcarka Cave (Moravian Karst) during a period of limited ventilation

Marek Lang¹, Jiří Faimon¹, and Camille Ek²

¹Department of Geological Sciences, Faculty of Sciences, Masaryk University, Kotlářská 2, 611 37 Brno, Czech Republic

²Department of Geology, University of Liège, 4000 Liège, Belgium

Abstract: The evolution of CO₂ levels with and without human presence was studied in a selected site (Gallery Chamber) of the homothermic zone of the Balcarka Cave (Moravian Karst, Czech Republic) during the fall, a period of limited ventilation. There were recognized various factors controlling the cave CO₂ levels under different conditions in the exterior and interior. When visitors were absent, CO₂ levels were controlled by the advective CO₂ fluxes linked to cave airflows and reaching up to $\sim 1.5 \times 10^{-3} \text{ mol s}^{-1}$. These fluxes exceed by orders of magnitude the exchanged diffusive fluxes (up to $4.8 \times 10^{-8} \text{ mol s}^{-1}$) and also the natural net flux (from 1.7×10^{-6} to $6.7 \times 10^{-6} \text{ mol s}^{-1}$) imputing given chamber directly from overburden. The natural net flux, normalized to unitary surface area, was estimated to be 2.8×10^{-8} to $1.1 \times 10^{-7} \text{ mol m}^{-2} \text{ s}^{-1}$, based on a perpendicular projection area of the chamber of $\sim 60 \text{ m}^2$. When visitors were present, the anthropogenic CO₂ flux into the chamber reached up to $3.5 \times 10^{-3} \text{ mol s}^{-1}$, which slightly exceeded the advective fluxes. This flux, recalculated per one person, yields the value of $6.7 \times 10^{-5} \text{ mol s}^{-1}$. The calculations of reachable steady states indicate that anthropogenic fluxes could almost triple the natural CO₂ levels if visitors stayed sufficiently long in the cave.

Keywords: anthropogenic and natural CO₂; cave ventilation; flux; dynamic model; temperature difference
 Received 11 July 2014; Revised 30 January 2015; Accepted 2 March 2015

Citation: Lang M., Faimon J. and Ek C., 2015. The relationship between carbon dioxide concentration and visitor numbers in the homothermic zone of the Balcarka Cave (Moravian Karst) during a period of limited ventilation. *International Journal of Speleology*, 44 (2), 167-176. Tampa, FL (USA) ISSN 0392-6672 <http://dx.doi.org/10.5038/1827-806X.44.2.6>

INTRODUCTION

Carbon dioxide (CO₂) is a key component controlling the karst processes such as limestone dissolution and calcite speleothem growth (Dreybrodt, 1999). The driving force for the latter process is the difference in the CO₂ partial pressure between (1) the soil/upper epikarst, $^{(E)}P_{\text{CO}_2}$, and (2) the cave atmosphere, $^{(C)}P_{\text{CO}_2}$ (White, 1998; Ford & Williams, 2007). Whereas a high $^{(E)}P_{\text{CO}_2}$ (Fairchild et al., 2000; Faimon et al., 2012a) controls saturation of percolating water with respect to the calcite, the lower $^{(C)}P_{\text{CO}_2}$ is responsible for dripwater degassing (releasing of the CO₂ excess) (Holland et al., 1964).

The instantaneous CO₂ concentration in the cave atmosphere is the balance of the input and output fluxes. The input CO₂ flux may generally include the direct natural fluxes associated with (i) the diffusion from soils/epikarst, (ii) dripwater degassing (Bourges et al., 2001), perhaps (iii) microbial decay of organic matter in cave sediments, and (iv) the transport of endogenous CO₂ in geologically active regions (Batiot-

Guilhe et al., 2007). The indirect CO₂ fluxes can be derived from air advection from (v) adjacent cave passages/epikarst, or e.g. (vi) a cave river and conduit flow. The anthropogenic flux is connected with (vii) the exhaling of cave visitors (Faimon et al., 2006; Milanolo & Gabrovšek, 2009). The output flux is linked with cave airflow and controlled by cave ventilation (Spötl et al., 2005; Banner et al., 2007; Baldini et al., 2008; Fernández-Cortés et al., 2009).

The cave airflow depends on (1) the cave geometry and (2) the pressure difference resulting from contrasting air densities (de Freitas et al., 1982). Since density is particularly a function of temperature, cave airflows are mostly related to the temperature difference $\Delta T = T_{\text{exterior}} - T_{\text{cave}}$ (where T_{exterior} is external air temperature and T_{cave} is cave air temperature [°C]) (de Freitas et al., 1982; Baker & Genty, 1998; Pflitsch & Piasecki, 2003; Russell & MacLean, 2008; Kowalczyk & Froelich, 2010; Faimon et al., 2012b). A theoretical background on cave air circulation was given by Cigna (1968) and Wigley & Brown (1971). Based on their geometry, caves may be sorted into two extreme

groups: (1) static caves with one entrance and (2) dynamic caves with two or more entrances at different altitudes (Geiger, 1966; Bögli, 1978). Whereas the static caves are ventilated for half of the season, the dynamic caves ventilate during the whole year by a so-called chimney effect. The transition between static caves and dynamic caves is represented by a statodynamic cave, defined by more than one entrance at the same altitude (Luetscher & Jeannin, 2004b). Some parts of the cave have features of a static cave, whereas other parts behave as a dynamic cave. If $\Delta T < 0$, upward airflows occur in the cave, i.e., external air enters the cave at the lower entrance and flows out from the cave by the upper entrance. This regime is called the upward airflow ventilation mode (UAF mode). If $\Delta T > 0$, cave airflows move in the opposite way. In this case, we talk about the downward airflow ventilation mode (DAF mode) (see Faimon et al., 2012a for details). According to the extent of temperature variations in the cave environment, (1) heterothermic zones (passages closer to cave entrances) and (2) homothermic zones (deeper cave passages) are defined (Luetscher & Jeannin, 2004b). Whereas the heterothermic zone is strongly influenced by external temperature, the homothermic zone is characterized by temperature stability. Two different ventilation periods can be distinguished in cave: (i) the period of active ventilation and (ii) the period of limited ventilation (Faimon et al., 2012b). In the active ventilation period, the duration of the individual ventilation mode exceeds the air residence time in the cave. In such a case, the air in the whole cave is completely exchanged. In the limited ventilation period, the duration of the actual ventilation mode is shorter than the air residence time in the cave. Then the direction of the airflow turns before the cave air is completely replaced by air from the external atmosphere (only the cave-entering passages are ventilated). Previous works on anthropogenically-impacted cave CO_2 were presented by, e.g., Pulido-Bosch et al. (1997), Song et al. (2000), Faimon et al. (2006), Liñán et al. (2008), Fernández-Cortés et al. (2009), Milanolo & Gabrovšek (2009) or Lario & Soler (2010). In this work, we focus on the anthropogenically-impacted CO_2 in the homothermic zone of the Balcarka Cave, a dynamic cave in the Moravian Karst (Czech Republic). The study was conducted when the ventilation modes changed diurnally and when the cave persisted in the period of limited ventilation. The goal of this work was to propose the dynamic model that would simulate evolution of cave CO_2 levels based on routinely available data: temperatures and visitor

numbers. The model aims at contributing to a better knowledge of the parameters controlling CO_2 levels in a visiting cave under specific conditions of changing ventilation. Overall, the article could help in better understanding recent karst processes.

SITE OF STUDY

The site of study, the Balcarka Cave, is situated in the northern part of the Moravian Karst near the village of Ostrov u Macochy (Faimon et al., 2012c). The sketch map of the cave with characteristic sites and their positions at different altitudes is illustrated in Fig. 1a. The cave was formed in the Devonian limestone of the Macocha Formation. It consists of two levels of narrow corridors, totaling about 350 m in length with chambers rich in speleothem formations. The height distance between both cave levels is about 20 m. The overburden thickness reaches up ~40 m (Fig. 1b). The same distance is probably between the levels of the lowest and highest openings. The complex cave geometry with three known entrances and more hidden openings at different altitudes ensures the dynamic behavior of air circulation. The Gallery Chamber in deeper cave passages (in the second cave level) was chosen as the monitoring site (Fig. 1a).

Fig. 1. Balcarka Cave: the sketch map with its position (a) and the altitude diagram of the individual cave passages (b). The letters denote the monitoring sites from the diagram.

The site is part of the homothermic zone. The chamber volume was estimated to ~150 m³. The cave is seasonally open to tourists with a total attendance of 30,000 to 40,000 persons per year. In the area above the Balcarka Cave, three soil types were identified: Anthrosol, lithic Leptosol, and brown rendzic Leptosol based on the vegetation such as pastures, mixed forest, and karst meadows, respectively (see Faimon et al., 2012c for details). The annual temperature of the external atmosphere at the given site is of ~8°C. The total annual precipitation is ~700 mm.

The site is part of the homothermic zone. The chamber volume was estimated to ~150 m³. The cave is seasonally open to tourists with a total attendance of 30,000 to 40,000 persons per year. In the area above the Balcarka Cave, three soil types were identified: Anthrosol, lithic Leptosol, and brown rendzic Leptosol based on the vegetation such as pastures, mixed forest, and karst meadows, respectively (see Faimon et al., 2012c for details). The annual temperature of the external atmosphere at the given site is of ~8°C. The total annual precipitation is ~700 mm.

METHODS

Data were collected during three monitoring campaigns between September and November 2013. A monitoring schedule is given in Table 1. In addition to the number of visitors, the cave CO₂ concentrations and the temperatures of cave air and external air were monitored. Airflow velocities were calculated from the temperature differences (see Faimon & Lang, 2013). Airflow direction was deduced from the sign

Table 1. Monitoring schedule (Balcarka Cave, Moravian Karst).

Monitoring Campaign	Date	Period [hours]	Number of tours	Visitors totally
Campaign I	28-30 Sept. 2013	48	16	265
Campaign II	19-21 Oct. 2013	48	11	176
Campaign III	2-4 Nov. 2013	48	6	124

of temperature differences and checked at the cave door positions. The CO₂ concentration was measured in the Gallery Chamber at 1 meter above the cave floor. It was detected by a 2-channel IR-detector FT A600-CO2H (measuring range: 0 to 10,000 ppmv; accuracy: ± 50 ppmv + 2 vol. % of measured value in the range of 0 to 5000 ppmv; resolution: 1 ppmv or 0.0001 vol. %) linked to the ALMEMO 2290-4 V5 Ahlborn data logger (Germany). The volume concentrations (in ppmv units) were subsequently recalculated into molar concentration (mol m⁻³), based on the Ideal Gas Law and given temperature and pressure,

$$c_{\text{CO}_2} [\text{mol m}^{-3}] = \frac{P}{10^6 RT} c_{\text{CO}_2} [\text{ppmv}] \quad (1)$$

where P is barometric pressure [Pa], R is the universal gas constant [$R = 8.3144621 \text{ J kg}^{-1} \text{ K}^{-1}$] and T is temperature [K].

The temperature was logged (i) in the exterior, about 50 m outside the cave, and (ii) inside the cave, about 100 m from the cave entrance. It was measured by COMET S3120 dataloggers (measuring range from -30 to +70°C with a precision of $\pm 0.4^\circ\text{C}$) (TR Instruments Inc., Czech Republic).

The variables were logged at 1-minute step (Campaigns 1 and 3) and 2-minute step (Campaign 2). The number of visitors in an individual tour was registered before their entering the cave. The moment of visitor entry into the monitoring site (due to the visitor moving with guide's commentary) was delayed by 33 ± 0.1 minutes. The length of stay in the site was 5-20 minutes (8.1 ± 5.9 min on average), based on the guide's commentary and visitor number. The initial time of interaction of visitors with the cave environment and the length of stay were finely tuned so that they were consistent with the CO₂ concentration peak. The sensitivity analysis was conducted using the program TopRank 6 (2014).

RESULTS

Monitoring Campaign I

During Campaign I, covering a total of 48 hours (see Table 1 for details), the monitoring was conducted at a temperature difference, $\Delta T = T_{\text{external}} - T_{\text{cave}}$, ranging between -8.8 and 4.9°C (Fig. 2c). Two ventilation modes were identified/predicted: (1) downward airflow ventilation mode (DAF) at positive ΔT and (2) upward airflow ventilation mode (UAF) at negative ΔT . The CO₂ concentrations in the chamber varied in a wide range depending on the temperature difference and the number of visitors (Fig. 2a). During the DAF modes, enhanced CO₂ concentrations of about $3.45 \times 10^{-2} \text{ mol m}^{-3}$ (800 ppmv) on average were registered. Sharp peaks of the values superimposed on "natural" CO₂ levels correspond very well to attendance and represent the anthropogenic impact on the CO₂ concentrations in the chamber. The heights of peaks corresponded to (i) the number of visitors in individual tours and (ii) staying period in the chamber. In the case of maximum attendance (52 visitors), the peak CO₂ concentration reached up to $5.83 \times 10^{-2} \text{ mol m}^{-3}$ (1350 ppmv). During the UAF mode, no visitors stayed in the cave. The CO₂ concentrations decreased to $2.50 \times 10^{-2} \text{ mol m}^{-3}$ (578 ppmv) on average.

Monitoring Campaign II

This 48-hour campaign (see Table 1) ran at a temperature difference ΔT varying from -9.8 to 10.4°C (Fig. 3c). The CO₂ concentrations varied depending on the temperature difference (DAF mode or UAF mode) and the number of visitors (Fig. 3a). During

Fig. 2. Monitoring of Campaign I (28-30 September 2013; Gallery Chamber, Balcarka Cave). There are data on CO₂ concentrations (the red line represents modeled curve) (a), visitor numbers (b), and temperature difference ΔT (c). See text for details.

Fig. 3. Monitoring of Campaign II (19-21 October 2013; Gallery Chamber, Balcarka Cave). There are data on CO₂ concentrations (the red line represents modeled curve) (a), visitor numbers (b), and temperature difference ΔT (c). See text for details.

the DAF modes, natural CO₂ concentrations varied about $3.00 \times 10^{-2} \text{ mol m}^{-3}$ (700 ppmv). The peak values corresponding to 37 visitors reached up to $4.52 \times 10^{-2} \text{ mol m}^{-3}$ (1040 ppmv). During the UAF mode (without visitors), the CO₂ concentrations decreased to $2.60 \times 10^{-2} \text{ mol m}^{-3}$ (600 ppmv).

Monitoring Campaign III

This 48-hour campaign (see Table 1) ran at a temperature difference ΔT ranging from -8.7 to 1.4°C (Fig. 4c). The resulting CO₂ concentrations in the chamber varied in a narrow range depending on the temperature difference and the number of

Fig. 4. Monitoring of Campaign III (2-4 November 2013; Gallery Chamber, Balcarka Cave). There are data on CO₂ concentrations (the red line is modeled curve) (a), visitor numbers (b), and temperature difference ΔT (c). See text for details.

visitors (Fig. 4a). During the DAF modes, natural CO₂ concentrations varied about $3.00 \times 10^{-2} \text{ mol m}^{-3}$ (693 ppmv) on average. The peak values (at 32 visitors) reached up to $3.68 \times 10^{-2} \text{ mol m}^{-3}$ (850 ppmv). During the UAF mode, when no visitors were in the cave, CO₂ concentrations decreased to $2.50 \times 10^{-2} \text{ mol m}^{-3}$ (578 ppmv).

DATA ANALYSIS

To evaluate the significant variables/parameters driving the CO₂ concentrations and to better understand the relations between them, a dynamic model was proposed that would simulate the evolution of CO₂ levels in the chamber. The model is based on the idea that the instantaneous CO₂ concentrations are given by balancing all the CO₂ fluxes into/out of the chamber. The conceptual model is depicted in Fig. 5. It consists of three reservoirs, the chamber of interest and two further adjacent spaces, and six fluxes among them: (1) the direct net natural flux into the Gallery Chamber from its overburden, j_N (associated with e.g. direct diffusion of CO₂ from soils/epikarst through the chamber roof and/or dripwater degassing), (2) the anthropogenic flux j_A (stemming from a person exhaling), (3) the advective input flux j_{adv}^{in} from an adjacent cave space (driven by ventilation), (4) the advective output flux from the chamber j_{adv}^{out} (driven by ventilation), (5) the diffusive input flux from an adjacent space j_{diff}^{in} , and (6) the diffusive output flux out of the chamber j_{diff}^{out} . Note that the advective input/output fluxes from/into adjacent spaces changed with each other with switching of the ventilation mode. The fluxes heading into the reservoir of interest (Gallery Chamber) are taken as positive, the fluxes heading out of the reservoir are negative. The total CO₂ flux into the reservoir, j [mol s^{-1}], is given by the sum of all individual fluxes,

$$j = \frac{dn_{\text{CO}_2}}{dt} = \frac{V dc}{dt} = \sum_i j_i \quad (2)$$

where n_{CO_2} is the total content of carbon dioxide in the chamber atmosphere [mol], t is time [s], V is the chamber volume [m^3], c is instantaneous CO₂ concentration in the chamber atmosphere [mol m^{-3}], and j_i are fluxes [mol s^{-1}].

The direct flux j_N was presumed to be constant during monitoring; it was found as one of the model parameters.

Anthropogenic CO₂ flux, j_A , was quantified as

$$j_A = k_A A \quad (3)$$

where k_A is a constant representing an anthropogenic personal flux [mol s^{-1}] and A is the attendance [number of visitors].

Fig. 5. Conceptual model of CO₂ dynamics in the atmosphere of the Gallery Chamber during the DAF ventilation mode (a) and UAF ventilation mode (b).

The advective fluxes, j_{adv}^{in} and j_{adv}^{out} , respectively, were expressed as a function of concentrations and airflows:

$$j_{adv}^{in} = v c_{adj} \quad (4)$$

and

$$j_{adv}^{out} = -v c \quad (5)$$

where v is the volumetric velocity of airflow through the cave chamber [$\text{m}^3 \text{s}^{-1}$], c is CO₂ concentration in the chamber [mol m^{-3}], and c_{adj} is CO₂ concentration in the relevant adjacent cave space serving as a sourcing reservoir [mol m^{-3}]. As c_{adj} , $c_{adj}^{(2)}$ was applied for the DAF ventilation mode and $c_{adj}^{(1)}$ was used for the UAF mode. Based on Faimon & Lang (2013), the volumetric airflow was calculated from temperature differences,

$$v = k_{AT} \sqrt{|\Delta T|} \quad (6)$$

where $\Delta T = T_{\text{exterior}} - T_{\text{cave}}$ [$^{\circ}\text{C}$] and k_{AT} is a proportionality constant [$\text{m}^3 \text{s}^{-1} \text{deg}^{-1/2}$].

The input and output diffusive fluxes, j_{dif}^{in} , and j_{dif}^{out} , respectively, were expressed as

$$j_{dif}^{in} = \frac{DS}{L} (c_{adj}^{(2)} - c) \quad (7)$$

and

$$j_{dif}^{out} = -\frac{DS}{L} (c - c_{adj}^{(1)}) \quad (8)$$

where D is a diffusion coefficient of CO₂ in the cave atmosphere [$\text{m}^2 \text{s}^{-1}$], S is the cave cross-section [m^2], and L is the distance, for which the concentration gradient, Δc [m], is given. Eqns. (7) and (8) are relevant for both the DAF and UAF modes.

Based on expected reasonable values of parameters, $D \sim 1.36 \times 10^{-5} \text{ m}^2 \text{s}^{-1}$ (Welty et al., 2008), $S \sim 10 \text{ m}^2$, $L \sim 100 \text{ m}$, $v \sim 0.04 \text{ m}^3 \text{s}^{-1}$, $V \sim 150 \text{ m}^3$, $c_{adj}^{(1)} \sim 1.7 \times 10^{-2} \text{ mol m}^{-3}$, $c \sim 3\text{--}6 \times 10^{-2} \text{ mol m}^{-3}$, $c_{adj}^{(2)} \sim 2\text{--}4 \times 10^{-2} \text{ mol m}^{-3}$, the advective fluxes vary in the range of $(1.1\text{--}1.5)$

$\times 10^{-3} \text{ mol s}^{-1}$, whereas the diffusive fluxes do not reach the values of $4.8 \times 10^{-8} \text{ mol s}^{-1}$.

Inserting all the fluxes into eqn. (2) and rearranging gives

$$\frac{dc}{dt} = \frac{k_A A}{V} + \frac{j_N}{V} + \frac{k_{AT} \sqrt{|\Delta T|}}{V} (c_{adj}^{(2)} - c) + \frac{DS}{LV} (c_{adj}^{(2)} - 2c + c_{adj}^{(1)}) \quad (9)$$

for the DAF ventilation mode. Eqn. (9) changes into

$$\frac{dc}{dt} = \frac{k_A A}{V} + \frac{j_N}{V} + \frac{k_{AT} \sqrt{|\Delta T|}}{V} (c_{adj}^{(1)} - c) + \frac{DS}{LV} (c_{adj}^{(2)} - 2c + c_{adj}^{(1)}) \quad (10)$$

in the case of the UAF mode, due to change in the input advective flux j_{adv}^{in} .

For both the ventilation modes, eqns. (9) and (10) were solved numerically. The little significant diffusive fluxes (the last terms in eqns. 9 and 10) were ignored in modeling for simplicity. Initially, values of the model parameters (j_N , c_{adj} , k_A , k_{AT}) were roughly set by trial and error so that the model curve best fit the data set. Important criteria for such fitting were (1) correspondence of data with the model at ΔT maxima/minima and at $\Delta T = 0$ in the periods without visitors and (2) heights of the CO₂ peaks at visitor presence. Consecutively, detail values of the parameters were exactly determined by the least square method. The loss function was minimized by the Levenberg-Marquardt method (Marquardt, 1963). Results of the modeling are presented in Figs. 2, 3, and 4 as thick red lines; the found regression parameters are given in Table 2.

Table 2. Regression parameters resulting from the modeling of individual monitoring campaigns (Gallery Chamber, Balcarka Cave).

Parameters	Values		
	Campaign 1	Campaign 2	Campaign 3
j_N [mol s^{-1}]	6.67×10^{-6}	1.67×10^{-6}	5.00×10^{-6}
$c_{adj \text{ DAF1}}$ [mol m^{-3}]	3.00×10^{-2}	2.95×10^{-2}	2.65×10^{-2}
$c_{adj \text{ DAF2}}$ [mol m^{-3}]	3.30×10^{-2}	3.20×10^{-2}	2.70×10^{-2}
$c_{adj \text{ UAF1}}$ [mol m^{-3}]	2.43×10^{-2}	2.40×10^{-2}	2.50×10^{-2}
$c_{adj \text{ UAF2}}$ [mol m^{-3}]	n.u.	2.55×10^{-2}	2.25×10^{-2}
$c_{adj \text{ UAF3}}$ [mol m^{-3}]	n.u.	2.80×10^{-2}	n.u.
k_A [mol s^{-1}]	6.67×10^{-5}	4.00×10^{-5}	5.33×10^{-5}
$k_{AT \text{ DAF}}$ [$\text{m}^3 \text{s}^{-1} \text{deg}^{-1/2}$]	1.50×10^{-2}	1.67×10^{-2}	4.83×10^{-2}
$k_{AT \text{ UAF}}$ [$\text{m}^3 \text{s}^{-1} \text{deg}^{-1/2}$]	7.30×10^{-3}	7.47×10^{-3}	5.83×10^{-3}

n.u. - not used

The c_{adj} concentrations varied in the range of $(2.65\text{--}3.30) \times 10^{-2} \text{ mol m}^{-3}$ (i.e., 620–770 ppmv) during the DAF mode and $(2.25\text{--}2.8) \times 10^{-2} \text{ mol m}^{-3}$ (530–660 ppmv) during the UAF mode. The k_{AT} values were determined in the range of $(1.50\text{--}4.83) \times 10^{-2} \text{ m}^3 \text{s}^{-1} \text{deg}^{-1/2}$ (DAF mode) and $(5.83\text{--}7.47) \times 10^{-3} \text{ m}^3 \text{s}^{-1} \text{deg}^{-1/2}$ (UAF mode). The calculated advective fluxes, j_{adv} , (see Table 3) were consistent with those $(1.1\text{--}1.5) \times 10^{-3} \text{ mol s}^{-1}$ estimated former.

The k_A values were found in the narrow range of $(4.00\text{--}6.67) \times 10^{-5} \text{ mol s}^{-1}$ (Table 2). Based on eqn. (6) and the number of visitors (Fig. 2–4), the instantaneous anthropogenic CO₂ fluxes, j_A , varied in the ranges: 6.0×10^{-4} to $3.5 \times 10^{-3} \text{ mol s}^{-1}$ (campaign I), 1.2×10^{-4} to $1.5 \times 10^{-3} \text{ mol s}^{-1}$ (campaign II), and 6.9×10^{-4} to $1.7 \times 10^{-3} \text{ mol s}^{-1}$ (campaign III) (Table 3).

Table 3. Overview of CO₂-fluxes based on modeling (Gallery Chamber, Balcarka Cave).

Flux	Campaign 1	Campaign 2	Campaign 3
j_A [mol s ⁻¹]	6.0×10^{-4} to 3.5×10^{-3}	1.2×10^{-4} to 1.5×10^{-3}	6.9×10^{-4} to 1.7×10^{-3}
$j_{adv}^{(in)}$ [mol s ⁻¹]	up to 1.1×10^{-3}	up to 1.5×10^{-3}	up to 1.3×10^{-3}
j_{dif} [mol s ⁻¹]	up to 4.8×10^{-8}	up to 2.7×10^{-8}	up to 1.6×10^{-8}

Direct natural flux (j_N) varied in the range of $(1.67\text{--}6.67) \times 10^{-6}$ mol s⁻¹. All fluxes are summarized in Tables 2 and 3. The chamber total volume $V \sim 150$ m³ was used for modeling.

The maximum reachable CO₂ concentration under given conditions is consistent with the steady state, at which the change of concentration in the chamber is zero, $dc/dt = 0$. For the DAF ventilation mode, during which visitors are in the cave, eqn. (9) yields

$$\frac{k_A A}{V} + \frac{j_N}{V} + \frac{k_{\Delta T} \sqrt{|\Delta T|}}{V} (c_{adj}^{(2)} - c^{ss}) + \frac{DS}{LV} (c_{adj}^{(2)} - 2c^{ss} + c_{adj}^{(1)}) = 0 \quad (11)$$

and after rearranging,

$$c^{ss} = \frac{j_N L + k_A A L + k_{\Delta T} L \sqrt{|\Delta T|} c_{adj}^{(2)} + DS(c_{adj}^{(2)} + c_{adj}^{(1)})}{k_{\Delta T} L \sqrt{|\Delta T|} + 2DS} \quad (12)$$

where c^{ss} is a steady state of CO₂ concentration in the chamber [mol m⁻³].

The effect of the relevant variables (ΔT and A) and key parameters (j_N and c_{adj}) on the cave CO₂ concentrations was tested by the standard sensitivity analysis. Generally, the method is used for assessing the contribution of individual driving variables/parameters to the increment/decrement of the dependent variable (see Saltelli et al., 2004). The analysis was applied to eqn. (12), in which the achievable CO₂ level, i.e., the steady state concentration, c^{ss} , is a function of relevant driving variables/parameters. The calculation was based on the average values of the $k_A = 5.3 \times 10^{-5}$ mol s⁻¹ and $k_{\Delta T} = 2.67 \times 10^{-2}$ m³ s⁻¹ deg^{-1/2} (found by modeling) and the values used for the flux estimating ($D \sim 1.36 \times 10^{-5}$ m² s⁻¹, $S \sim 10$ m², $L \sim 100$ m, $v \sim 0.04$ m³ s⁻¹, $V \sim 150$ m³, and $c_{adj}^{(1)} \sim 1.7 \times 10^{-2}$ mol m⁻³). The individual inputs for the analysis covered the range of parameters/variables found by modeling (Table 2). Results of the sensitivity analysis are presented in Fig. 6. During the natural regime without visitors ($A = 0$), the concentrations in adjacent spaces, c_{adj} , have the most significant effect on CO₂ levels (Fig. 6a). The effect of the temperature difference ΔT and direct natural flux (j_N) are either small or almost negligible, respectively. For the regime with visitors, the results are very different: the CO₂ levels are extremely affected by ΔT (Fig. 6b). The variations in ΔT may almost triple the CO₂ level in the chamber in comparison with the visitor number (A) and even quadruple in comparison with the adjacent space concentrations, $c_{adj}^{(2)}$. The role of the direct natural flux is similarly insignificant as in the regime without visitors. In the case of $\Delta T \gg 0$, the effect of ΔT diminishes (Fig. 6c).

DISCUSSION

The natural CO₂ concentrations between 2×10^{-2} and 3×10^{-2} mol m⁻³ (460 and 700 ppmv) found in the

Fig. 6. Sensitivity analysis: evolution of the CO₂ steady state concentrations in the cave chamber based on the variation of individual parameters. The case without visitors (a); the case with visitors at different temperature ranges (b, c).

Balcarka Cave are roughly consistent with the values reported by Spötl et al. (2005) for the Obir Caves (Austria), Baldini et al. (2006) for the Ballynamintra Cave (Ireland) or with those measured by Liñán et al. (2008) in the Nerja Cave (Spain). In contrast, these values are substantially lower than the values of 0.24 mol m⁻³ (5,500 ppmv) reported by Buecher (1999) for the Kartchner Caverns (Arizona), 0.36 mol m⁻³ (8,300 ppmv) presented by Ek & Gewelt (1985) in the Ste-Anne Cave (Belgium), 1.8 mol m⁻³ (41,500 ppmv) reported by Bourges et al. (2001) or even 2.68 mol m⁻³ (62,000 ppmv) given by Batiot-Guilhe et al. (2007) (Causse d'Aumelas, France). This comparison indicates that the Balcarka Cave belongs to the caves with rather low CO₂ levels. The peak CO₂ values up to 6×10^{-2} mol m⁻³ (1,400 ppmv) linked to the anthropogenic impact are comparable with the values referred by Dragovich & Grose (1990), Faimon et al. (2006) or Benavente et al. (2011). On the other hand, they do not reach the value ~ 0.1 mol m⁻³ (2,300 ppmv) presented by Milanolo & Gabrovšek (2009). Nevertheless, the anthropogenic impact on the Balcarka Cave environment may be classified as a standard one in comparison with other visiting caves. During all the monitoring campaigns, the cave persisted in the so-called *fall period of limited ventilation* (Faimon et al., 2012a). This *period* follows the *summer period of active ventilation* that provided enhanced CO₂ levels.

Natural influence

The sensitivity analysis (Fig. 6), the preliminary calculations based on eqns. (3) to (8), and the modeling

results (Fig. 3-4, Table 2) showed that natural CO₂ levels in the chamber (in the case without visitors) are controlled by the advective CO₂ fluxes from adjacent cave spaces. These fluxes are a function of (1) CO₂ concentrations in these spaces, c_{adj} , and (2) cave airflows controlled by temperature difference, $\Delta T = T_{\text{exterior}} - T_{\text{cave}}$, (Fig. 6a). Based on airflow direction (controlled by the ΔT sign), different CO₂ fluxes enter the chamber from different adjacent spaces. The lesser CO₂ concentrations are results of the fluxes from the spaces situated below, closer to the cave entrance (operating as an inputting reservoir during the UAF mode, see Fig. 5a). The higher CO₂ concentrations are transported by the fluxes from deeper/higher-situated cave spaces (operating as an inputting reservoir during the DAF mode, see Fig. 5b). The concentrations $c_{adj}^{(2)}$ are probably derived from soil/epikarstic CO₂; it is even conceivable that the concentrations represent the CO₂ directly “soaked” from the epikarst. Various sinkholes and shafts filled with porous sediment and representing a section into the karst’s vertical profile may serve as the entrances for such transport. Peak values of the CO₂ concentrations measured in the soils above the Balcarka Cave reach up to 4,500 ppmv (Faimon et al., 2012c). Under the correction for the drill-hole diameter at monitoring (Blecha & Faimon, 2014), the peak values could even reach up to ~6,000 ppmv ($2.6 \times 10^{-1} \text{ mol m}^{-3}$). Such values should fully cover the concentrations predicted by the model, $\sim 3 \times 10^{-2} \text{ mol m}^{-3}$ (Table 2). It should be emphasized that the CO₂ concentrations in the adjacent space, $c_{adj}^{(2)}$, were not available for direct monitoring because of (1) uncertainty in the airflow path and (2) inaccessibility of such spaces. The $c_{adj}^{(1)}$ values predicted by the model, $2.2\text{--}2.8 \times 10^{-2} \text{ mol m}^{-3}$ (500–650 ppmv) (Table 2) are in good agreement with the values of about $2.3 \times 10^{-2} \text{ mol m}^{-3}$ (530 ppmv) ordinarily measured at the entrance passages of the cave. From the c_{adj} variations during the campaigns and even during individual monitoring periods (Table 2), it is evident that the parameter is not invariant. However, the 8.8% variation (variation coefficient) during the DAF mode and 7.4% variation during the UAF mode seem to be reasonable and expectable/acceptable ones considering the capacities of CO₂ source and outgoing fluxes.

Similarly to c_{adj} , data on the actual airflows and its directions were not available. The reason was its extremely low linear velocity and technical difficulties during their monitoring. Therefore, the airflows and their directions were estimated from temperature differences based on eqn. (5) and sign of ΔT , respectively (see Faimon & Lang, 2013 for details). Based on the regression analysis, the values of k_{AT} were found to vary in the range of $(5.83\text{--}7.47) \times 10^{-3} \text{ m}^3 \text{ s}^{-1} \text{ deg}^{-1/2}$ for the UAF mode and $(1.50\text{--}4.83) \times 10^{-2} \text{ m}^3 \text{ s}^{-1} \text{ deg}^{-1/2}$ for the DAF mode (Table 2). Similar values were found for the Císařská Cave (Moravian Karst) in the UAF mode, but much lesser ones for the same site in the DAF mode (Faimon & Lang, 2013). In fact, k_{AT} is expected to vary with cave geometry, especially the difference in altitudes of entrances, or length and diameters of the conduits.

The switching between DAF and UAF ventilation modes is principally expected at zero ΔT , when both the cave and external temperatures are balanced. However, the modeling results indicate that the mode switching could be achieved at non-zero ΔT . This phenomenon was published by, e.g., de Freitas et al. (1982) or Faimon et al. (2012b), who estimated the switching ΔT in the range of 0.6 to 1.4°C. The modeling showed comparable values: the individual ventilation modes in the Gallery Chamber most likely switched at $|\Delta T|$ ranging from 0.4 to 3.2 °C (Fig. 3 and 4). This discrepancy may be the result of the non-uniform distribution of temperatures, humidity, and CO₂ concentrations throughout the cave (Faimon & Lang, 2013; Sánchez-Cañete et al., 2013).

The modeling showed that it was potentially suitable for distinguishing the direct net natural fluxes into the chamber from overburden, j_N . Generally, the flux should induce the increment of CO₂ levels at/near zero ΔT , when the CO₂ concentrations in the chamber are not lowered by ventilation. However, the data do not indicate such an effect. The extremely low flux j_N of the orders of $10^{-6} \text{ mol s}^{-1}$ was identified (Table 2). The flux is much lower than the advective fluxes (up to $1.5 \times 10^{-3} \text{ mol s}^{-1}$). This could mean that (1) CO₂ fluxes into the cave are distributed un-uniformly following predominant paths, and (2) water degassing in the site is not a dominant source. The rather highest j_N value from the observed range that was found during Campaign I (September) might be a residuum of enhanced CO₂ production during the end of the summer season. Despite the possible un-uniform distribution, the flux j_N was approximately recalculated into the specific flux normalized to a 1 m² area. Based on the orthogonal projection plane of the chamber of about 60 m², such a flux would correspond to the values from 2.8×10^{-8} to $1.1 \times 10^{-7} \text{ mol m}^{-2} \text{ s}^{-1}$. These values are consistent with $7.59 \times 10^{-8} \text{ mol m}^{-2} \text{ s}^{-1}$ presented for the Císařská Cave by Faimon et al. (2006). On the other hand, the value is much lower in comparison with $1 \times 10^{-5} \text{ mol m}^{-2} \text{ s}^{-1}$ presented by Milanolo & Gabrovšek (2009).

Anthropogenic influence

According to modeling, the peak anthropogenic CO₂ flux into the chamber, j_A , reached $3.5 \times 10^{-3} \text{ mol s}^{-1}$ depending on the number of visitors. Even though it is a rather higher flux in the modeled system (Table 3), it does not reach the maxima of the natural advective fluxes. The sensitivity analysis showed the extremely strong effect of ΔT on the resulting cave CO₂ concentrations (Fig. 6b). The reason is that cave ventilation and outputting fluxes are suppressed during the periods at $|\Delta T| \sim 0^\circ\text{C}$, when the chamber CO₂ levels are only limited by small diffusive fluxes. From a mathematical point of view, the low value of the denominator in eqn. (12) at $\Delta T = 0^\circ\text{C}$ causes an extreme increase in the c^{ss} value. However, the time periods when the cave persists at zero ΔT are very short, as is visible in the ΔT data (Fig. 2c-4c). This short time does not allow neither reaching the steady state concentrations, c^{ss} , nor a significant increase

of the CO₂ level in the chamber. For example, data from Campaign I indicate that the $|\Delta T|$ values are in the range of 0.7 to 8°C for 90% of the time of the monitored period. During this time, the effect of ΔT is significantly lower; it is comparable with the visitor effect (see Fig. 6c).

The k_A constant (see Table 1) corresponds to an individual personal flux, $j_A^{(\text{personal})}$. The mean value, $j_A^{(\text{personal})} \sim 6.7 \times 10^{-5} \text{ mol s}^{-1}$, is lower than the values of $2.9 \times 10^{-4} \text{ mol s}^{-1}$ presented by Faimon et al. (2006) or $(2.60\text{--}3.35) \times 10^{-4} \text{ mol s}^{-1}$ reported by Milanolo & Gabrovšek (2009). In general, factors causing differences in the values may be human age (Tormo et al., 2001; Faimon et al., 2006), activity (Iwamoto et al. 1994), and gender (Sciacca et al. 2002).

To quantify the potential anthropogenic impact, the CO₂ steady state, c^{ss} , was calculated for the maximum number of visitors (Campaign I). If a peak anthropogenic flux $j_A = 3.5 \times 10^{-3} \text{ mol s}^{-1}$ is assumed, a steady state concentration of $c^{ss} \sim 0.15 \text{ mol m}^{-3}$ (3471 ppmv) would be reached. This value is roughly comparable with the value presented by Faimon et al. (2006). It shows that the natural CO₂ level could almost be tripled under the condition that visitors were in cave for a sufficiently long period.

The present work should be understood as an attempt to simulate cave CO₂ levels based on (1) a limited/ordinary available data set and (2) a general knowledge on the art of cave microclimatology. The reason for limited data are principal difficulties at the direct measuring of (i) CO₂ concentrations at the adjacent sites and (ii) cave airflows. Therefore, all the missing parameters, j_N , c_{adj} , k_A , and k_{AT} , were found indirectly, by modeling. This led to the great fitting of the data by the model on one hand, however, to a limited verification of an inner mechanism of the model by direct measurement on the other hand. Nevertheless, we believe that our approach would be useful for other researchers as a basic tool for the study of cave CO₂ dynamics and that the model will be elaborated in greater detail in the future.

CONCLUSIONS

The evolution of CO₂ concentrations was studied in the homothermic zone of the Balcarka Cave, the visiting cave in Moravian Karst (Czech Republic) during the fall period of limited ventilation. The results showed that CO₂ levels in the studied cave site were controlled by different factors depending on given conditions in both the exterior and interior. When no visitors were present, the CO₂ levels in the chamber were controlled by CO₂ fluxes from adjacent cave spaces. These fluxes were controlled by (1) the adjacent spaces' CO₂ levels and (2) airflows driven by the temperature difference between the exterior and the cave site. When visitors were present, CO₂ levels at the site were significantly influenced by the anthropogenic flux dependent on the number of visitors. The immediate increment of CO₂ levels in the chamber depended on the duration of the visit. The model showed that the anthropogenically-impacted steady state concentrations would almost triple the

natural CO₂ levels when visitors stayed sufficiently on site. This indicates how reducing the period of a tour in the cave could substantially contribute to better protection of the cave environment.

The article represents a case study based on data coming from the late summer and fall, when the cave experienced the so-called "fall period of limited ventilation." This period is characterized by higher natural CO₂ levels deeper in the cave that have persisted from an enhanced summer CO₂ production. A similar study should be undertaken in the spring period of limited ventilation under the conditions of generally low natural CO₂ levels resulting from the winter period of active ventilation. Unfortunately, the cave is closed during the winter season, which did not allow the study of anthropogenic CO₂ behavior during the winter period of active ventilation. Nevertheless, further study during the summer period of active ventilation at enhanced natural CO₂ levels will be worthwhile. The study results may be useful for better cave management: based on our model, the numbers of visitors in groups and individual intervals between the visitor groups may be determined so that they burden the cave environment less in dependence of seasonal conditions. In general, the work may be of interest to karsologists and environmentalists.

ACKNOWLEDGEMENTS

The authors wish to thank three anonymous reviewers for valuable comments. Thank you to Peter Blackie and Philippe Labarbe for critically reading the manuscript. The research was supported by funding from the Masaryk University.

REFERENCES

- Baker A. & Genty D., 1998 - *Environmental pressures on conserving cave speleothems: effects of changing surface land use and increased cave tourism*. Journal of Environmental Management, **53**: 165-175.
<http://dx.doi.org/10.1006/jema.1998.0208>
- Baldini J.U.L., Baldini L.M., McDermott F. & Clipson N., 2006 - *Carbon dioxide sources, sinks, and spatial variability in shallow temperate zone caves: Evidence from Ballynamintra Cave, Ireland*. Journal of Cave and Karst Studies, **68**: 4-11.
- Baldini J.U.L., McDermott F., Hoffmann D.L., Richards D.A. & Clipson N., 2008 - *Very high-frequency and seasonal cave atmosphere PCO₂ variability: Implications for stalagmite growth and oxygen isotope-based paleoclimate records*. Earth and Planetary Science Letters, **272**: 118-129.
<http://dx.doi.org/10.1016/j.epsl.2008.04.031>
- Banner J.L., Guilfoyle A., James E.W., Stern L.A. & Musgrove M., 2007 - *Seasonal variations in modern speleothem calcite growth in Central Texas, USA*. Journal of Sedimentary Research, **77**: 615-622.
<http://dx.doi.org/10.2110/jsr.2007.065>
- Batiot-Guilhe C., Seidel J.-L., Jourde, H., Hébrard O. & Bailly-Comte V., 2007 - *Seasonal variations of CO₂ and ²²²Rn in a mediterranean sinkhole – spring (Causse d'Aumelas, SE France)*. International Journal of Speleology, **36** (1): 51-56.
<http://dx.doi.org/10.5038/1827-806X.36.1.5>

- Benavente J., Vadillo I., Liñan C., Carrasco F. & Soler A., 2011 - *Ventilation effects in a karstic show cave and in its vadose environment, Nerja, Southern Spain*. Carbonates and Evaporites, **26**: 11-17.
<http://dx.doi.org/10.1007/s13146-011-0050-9>
- Blecha M. & Faimon J., 2014 - *Karst soils: Dependence of CO₂ concentrations on pore dimension*. Acta Carsologica, **43** (1): 55-64.
- Bourges F., Mangin A. & d'Hulst D., 2001 - *Le gaz carbonique dans la dynamique de l'atmosphère des cavités karstiques: l'exemple de l'Aven d'Ornag (Ardèche)*. Carbon dioxide in karst cavity atmosphere dynamics: the example of the Aven d'Ornag (Ardèche). Earth and Planetary Sciences, **333**: 685-692.
- Bögli A., 1978 - *Karsthydrographie und physische Speleologie*. Springer, Berlin, 292 p.
- Buecher R.H., 1999 - *Microclimate study of Kartchner Caverns, Arizona*. Journal of Cave and Karst Studies, **61**: 108-120.
- Cigna A.A., 1968 - *An analytical study of air circulation in caves*. International Journal of Speleology, **3**: 41-54.
<http://dx.doi.org/10.5038/1827-806X.3.1.3>
- de Freitas C.R., Littlejohn R.N., Clarkson T.S. & Kristament I.S., 1982 - *Cave climate: assessment of airflow and ventilation*. Journal of Climatology, **2**: 383-397.
<http://dx.doi.org/10.1002/joc.3370020408>
- Dragovich D. & Grose J., 1990 - *Impact of tourists on carbon dioxide levels at Jenolan Caves, Australia: an examination of microclimatic constraints on tourist cave management*. Geoforum, **21**: 111-120.
[http://dx.doi.org/10.1016/0016-7185\(90\)90009-U](http://dx.doi.org/10.1016/0016-7185(90)90009-U)
- Dreybrodt W., 1999 - *Chemical kinetics, speleothem growth and climate*. Boreas, **28**: 347-356.
- Ek C. & Gewelt M., 1985 - *Carbon dioxide in cave atmospheres. New results in Belgium and comparison with some other countries*. Earth Surface Processes and Landforms, **10**: 173-187.
<http://dx.doi.org/10.1002/esp.3290100209>
- Faimon J., Štelcl J. & Sas D., 2006 - *Anthropogenic CO₂ flux into cave atmosphere and its environmental impact: a case study in the Císařská Cave (Moravian Karst, Czech Republic)*. Science of the Total Environment, **369**: 231-245.
- Faimon J., Ličbinská M., Zajiček P. & Sracek O., 2012a - *Partial pressures of CO₂ in epikarstic zone deduced from hydrogeochemistry of permanent drips, the Moravian Karst, Czech Republic*. Acta Carsologica, **41** (1): 47-57.
- Faimon J., Troppová D., Baldík V. & Novotný R., 2012b - *Air circulation and its impact on microclimatic variables in the Císařská Cave (Moravian Karst, Czech Republic)*. International Journal of Climatology, **32**: 599-623.
<http://dx.doi.org/10.1002/joc.2298>
- Faimon J., Ličbinská M. & Zajiček P., 2012c - *Relationship between carbon dioxide in Balcarka Cave and adjacent soils in the Moravian Karst region of the Czech Republic*. International Journal of Speleology, **41** (1): 17-28.
<http://dx.doi.org/10.5038/1827-806X.41.1.3>
- Faimon J. & Lang M., 2013 - *Variances in airflows during different ventilation modes in a dynamic U-shaped cave*. International Journal of Speleology, **42** (2): 115-122.
<http://dx.doi.org/10.5038/1827-806X.42.2.3>
- Fairchild I.J., Borsato A., Tooth A.F., Frisia S., Hawkesworth C.J., Huang Y., McDermott F. & Spiro B., 2000 - *Controls on trace element (Sr-Mg) compositions of carbonate cave waters: implications for speleothem climatic records*. Chemical Geology, **166**: 255-269.
[http://dx.doi.org/10.1016/S0009-2541\(99\)00216-8](http://dx.doi.org/10.1016/S0009-2541(99)00216-8)
- Fernández-Cortés A., Sánchez-Moral S., Cuezva S., Cañaveras J.C. & Abella R., 2009 - *Annual and transient signatures of gas exchange and transport in the Castañar de Ibor cave (Spain)*. International Journal of Speleology, **38** (2): 153-162.
<http://dx.doi.org/10.5038/1827-806X.38.2.6>
- Ford T.D. & Williams P.W., 2007 - *Karst Hydrogeology and Geomorphology*. Wiley & Sons, Chichester, 562 p.
- Geiger R., 1966 - *The climate near the ground*. Harvard University Press, Cambridge, 628 p.
- Holland H.D., Kirsipu T.V., Huebner J.S. & Oxburgh U.M., 1964 - *On some aspects of the chemical evolution of cave water*. Journal of Geology, **72**: 36-67.
<http://dx.doi.org/10.1086/626964>
- Iwamoto J., Pendergast D.R., Suzuki H. & Krasney J.A., 1994 - *Effect of graded exercise on nitric oxide in expired air in humans*. Respiration Physiology, **97**: 333-345.
[http://dx.doi.org/10.1016/0034-5687\(94\)90069-8](http://dx.doi.org/10.1016/0034-5687(94)90069-8)
- Kowalczyk A.J. & Froelich P.N., 2010 - *Cave air ventilation and CO₂ outgassing by radon-222 modeling: How fast do caves breathe?* Earth and Planetary Science Letters, **289**: 209-219.
<http://dx.doi.org/10.1016/j.epsl.2009.11.010>
- Lario J. & Soler V., 2010 - *Microclimate monitoring of Pozalagua Cave (Vizcaya, Spain): application to management and protection of show caves*. Journal of Cave and Karst Studies, **72** (3): 169-180.
<http://dx.doi.org/10.4311/jcks2009lsc0093>
- Liñan C., Vadillo I. & Carrasco F., 2008 - *Carbon dioxide concentration in air within the Nerja Cave (Malaga, Andalusia, Spain)*. International Journal of Speleology, **37**: 99-106.
<http://dx.doi.org/10.5038/1827-806X.37.2.2>
- Luetscher M. & Jeannin P.-Y., 2004b - *Temperature distribution in karst systems: the role of air and water fluxes*. Terra Nova, **16**: 344-350.
<http://dx.doi.org/10.1111/j.1365-3121.2004.00572.x>
- Marquardt D.W., 1963 - *An Algorithm for Least-Squares Estimation of Nonlinear Parameters*. Journal of the Society for Industrial and Applied Mathematics, **11** (2): 431-441.
<http://dx.doi.org/10.1137/0111030>
- Milanolo S. & Gabrovšek F., 2009 - *Analysis of Carbon Dioxide Variations in the Atmosphere of Srednja Bijambarska Cave, Bosna and Herzegovina*. Boundary-Layer Meteorology, **131**: 479-493.
<http://dx.doi.org/10.1007/s10546-009-9375-5>
- Pflitsch A. & Piasecki J., 2003 - *Detection of an airflow system in Niedzwiedzia (Bear) Cave, Kletno, Poland*. Journal of Cave and Karst Studies, **65**: 160-173.
- Pulido-Bosch A., Martín-Rosales W., López-Chicano M., Rodríguez-Navarro C.M. & Vallejos A., 1997 - *Human impact in a tourist karstic cave (Aracena, Spain)*. Environmental Geology, **31** (3/4): 142-149.
<http://dx.doi.org/10.1007/s002540050173>
- Russell M.J. & MacLean V.L., 2008 - *Management issues in a Tasmanian tourist cave: Potential microclimatic impacts of cave modifications*. Journal of Environmental Management, **87**: 474-483.
<http://dx.doi.org/10.1016/j.jenvman.2007.01.012>
- Sánchez-Cañete E.P., Serrano-Ortiz P., Domingo F. & Kowalski A.S., 2013 - *Cave ventilation is influenced by variations in the CO₂-dependent virtual temperature*. International Journal of Speleology, **42** (1): 1-8.
<http://dx.doi.org/10.5038/1827-806X.42.1.1>
- Saltelli A., Tarantola S., Campolongo F. & Ratto M., 2004 - *Sensitivity analysis in practice: A guide to assessing scientific models*. (1st ed.). John Wiley & Sons, Chichester, 232 p.

- Sciaccia J., Forbes W.M., Ashton F.T., Lombardini E., Gamble H.R. & Schad G.A., 2002 - *Response to carbon dioxide by the infective larva of three species of parasitic nematodes*. *Parasitology International*, **51**: 53-62.
[http://dx.doi.org/10.1016/S1383-5769\(01\)00105-2](http://dx.doi.org/10.1016/S1383-5769(01)00105-2)
- Song L., Wei X. & Liang F., 2000 - *The influences of cave tourism on CO₂ and temperature in Baiyun Cave, Hebei, China*. *International Journal of Speleology*, **29 B (1/4)**: 77-87.
- Spötl C., Fairchild I.J. & Tooth A.F., 2005 - *Cave air control on dripwater geochemistry, Obir Caves (Austria): implications for speleothem deposition in dynamically ventilated caves*. *Geochimica et Cosmochimica Acta*, **69 (10)**: 2451-2468.
<http://dx.doi.org/10.1016/j.gca.2004.12.009>
- TopRank 6, 2014 - *Automated „what-if“ Analysis for Spreadsheet*. Online: <http://www.palisade.com/toprank/> [20. 2. 2014]
- Tormo R., Bertaccini A., Conde M., Infante D. & Cura I., 2001 - *Methane and hydrogen exhalation in normal children and in lactose malabsorption*. *Early Human Development*, **65**: 165-172.
[http://dx.doi.org/10.1016/S0378-3782\(01\)00219-5](http://dx.doi.org/10.1016/S0378-3782(01)00219-5)
- White W.B., 1988 - *Geomorphology and hydrology of karst terrains*. Oxford University Press, New York, 464 p.
- Wigley T.M.L. & Brown M.C., 1971 - *Geophysical applications of heat and mass transfer in turbulent pipe flow*. *Boundary-Layer Meteorology*, **1**: 300-320.
<http://dx.doi.org/10.1007/BF02186034>
- Welty J.R., Wicks C.E., Wilson R.E. & Rorrer G.L., 2008 - *Fundamentals of momentum, heat, and mass transfer*. (5th ed.). John Wiley & Sons, Inc., New York, 729 p.