The Efficiency of Sampling Techniques for NTD Reporting

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Abstract

This paper examines the minimum sample size required by each of six sampling techniques for estimating annual passenger miles traveled to meet the Federal Transit Administration’s 95% confidence and 10% precision levels for the National Transit Database. It first describes these sampling techniques in non-technical terms and hypothesizes how they are expected to compare in their minimum sample sizes. It then determines the minimum sample size for 83 actual sample datasets that cover 6 modes and 65 transit agencies. Finally, it summarizes the results in minimum sample size to compare the relative efficiency of these sampling techniques. The potential for improved efficiency from using these sampling techniques is great, but the exact degree of improvement depends highly on individual agencies, modes, and services.

Introduction

To be eligible for the Urbanized Area Formula Grant Program of the Federal Transit Administration (FTA), transit agencies must report annual passenger miles traveled (PMT) to the Nation Transit Database (NTD) for each combination of mode and type of service (purchased or directly-operated) (FTA 2007, FTA 2008). The NTD requires that a 100% count of annual PMT be reported if it is available and reliable. Getting a 100% account of annual PMT, however, requires keeping track of the distance that every passenger travels. Except in a few cases (e.g., ferryboat with only two stops), annual PMT is almost always estimated through...
statistical sampling, and such an estimate must meet FTA’s 95% confidence and 10% precision levels.

To estimate annual PMT through random sampling, agencies have the burden of developing a sampling plan that meets FTA’s requirements, as well as the significantly higher burden of collecting the sample data. It is highly desirable to be able to reduce these agency costs while meeting FTA’s confidence and precision requirements.

One strategy to reduce agencies’ burden of developing sampling plans would be to have a user-friendly Excel template for individual agencies to explore and develop sampling plans that are most efficient for their conditions. One example can be found in Chu and Ubaka (2004), but the study was limited to the sampling technique used in FTA’s Circular 2710.1A for motorbus. Chu (2009) develops a more comprehensive template that incorporates a range of sampling techniques that agencies can explore. While the paper uses this new template for analysis, this strategy is not a focus and is not discussed further.

The most effective strategy to reduce agencies’ burden of data collection would be through improving sampling efficiency by taking advantage of modern sampling techniques. Furth (2005), for example, shows the capability of modern sampling techniques to improve sampling efficiency for one agency. This is the focus of this paper.

Many agencies, however, do not consider the relative efficiency of modern sampling techniques. The existence of the circular sampling plans for motorbus and demand-response may have discouraged agencies from seeking more efficient sampling plans (UMTA 1988a, UMTA 1988b). More important, agencies may not fully understand the potential cost savings. The literature does not have adequate information on these cost savings. The technical work in the literature typically includes actual examples of cost savings, but these examples are limited to a few cases (Furth 2005) or a few sampling techniques (Furth and McCollom 1987) and are almost always for motorbus only.

The goal of the paper is to encourage agencies to explore the potential of cost savings from using various modern sampling techniques. Toward that goal, the objective is to examine several modern sampling techniques and the potential of reducing agency costs from using them. Specifically, this paper provides the most comprehensive picture of how six modern sampling techniques may perform across a wide range of modes and operating conditions under a uniform process
for data analysis. This comprehensive picture helps transit agencies better understand the potential cost savings from using these sampling techniques. It also helps transit agencies better understand that the actual efficiency of individual sampling techniques and their relative efficiency depend highly on the mode and the actual operating conditions.

The remainder of the paper first describes six sampling techniques in non-technical terms and hypothesizes how they are expected to compare for their respective minimum sample sizes. It then determines the minimum sample size for 83 actual sample datasets that cover 6 modes and 65 transit agencies. Finally, it summarizes the results in minimum sample size to compare the relative efficiency of these sampling techniques. It also shows the potential and variations in the relative efficiency across the sample datasets used.

**Sampling Techniques**

Table 1 summarizes the six sampling techniques considered in this paper. One way to understand them is to look at them as defined by the two basic sampling methods listed in the columns and the three estimation methods listed in the rows. The description here avoids technical details, which are available in standard textbooks on sampling techniques (Cochran 1977).

<table>
<thead>
<tr>
<th>Estimation Methods</th>
<th>Basic Sampling Methods</th>
</tr>
</thead>
<tbody>
<tr>
<td>Basic Methods</td>
<td>Alternative Approaches</td>
</tr>
<tr>
<td>Direct Expansion</td>
<td>N/A</td>
</tr>
<tr>
<td>Ratio Expansion</td>
<td>Absolute APTL</td>
</tr>
<tr>
<td></td>
<td>Relative APTL</td>
</tr>
</tbody>
</table>

**Basic Sampling Methods**

Simple random sampling involves every unit operated having the same chance of being selected at random. Stratified sampling, on the other hand, involves dividing an agency’s service into two or more groups and sampling separately within each group. The objective of stratification is to reduce within-group differences.
For an agency that operates both local and express bus services, with the latter having much longer routes, for example, the average passenger trip length (APTL) is likely to vary less across local bus trips or across express bus trips than across all bus trips.

**Estimation Methods**

There are two basic methods to estimate PMT—direct expansion and ratio expansion. In the case of sampling one-way bus trips, direct expansion involves multiplying the average PMT per one-way bus trip in a sample with an expansion factor, or the total number of one-way bus trips actually operated in this case. FTA’s Circular 2710.1A is based on this expansion method for motorbus services (UMTA 1988a). Ratio expansion, on the other hand, involves multiplying the estimate of a ratio from a sample with a known quantity. Estimating PMT as the product of a 100% count of unlinked passenger trips (UPT) and an estimated APTL is one example of ratio expansion. In this case, the APTL is the ratio and the 100% count of UPT is the known quantity. FTA’s Circulars 2710.2A and 2710.4A are based on ratio expansion (UMTA 1988b, UMTA 1988c).

The paper considers two of the three approaches to ratio expansion that have appeared in the literature—one based on absolute APTL, one based on cash revenues, and one based on relative APTL. The approach based on absolute APTL is already mentioned above. The approach based on cash revenues uses PMT per dollar of cash-fare revenue as the ratio and total cash-fare revenues as the known quantity. FTA’s Circular 2710.4A is based on the revenue approach (UMTA 1988c) and, because of changing patterns in cash-fare payment over time, FTA no longer approves the sampling plan in this circular without certification by a qualified statistician. For the same reason, this paper does not consider the revenue approach any further.

Furth (2005) recently proposed the ratio-expansion approach based on relative APTL. This new approach uses a new known quantity called potential PMT. For any unit of operation along a route (i.e., one one-way vehicle trip, all operations in a year, etc.), its potential PMT is the product of the UPT count on that unit and the route length. In other words, the potential PMT for a given route is its PMT if every passenger traveled the full route length. This new approach uses a relative APTL from a sample as the ratio. For a given route, the relative APTL is the absolute APTL over the route length. The relative APTL for a route gives the average fraction of a route’s length that passengers travel on all units of service. A ratio of
0.5 for a route, for example, would indicate that, on average, passengers travel one half of the length of the route.

**Prerequisites**

Table 2 summarizes the prerequisites of these sampling techniques in terms of modes and required data. Direct simple random sampling is applicable to all situations. Each of the other techniques has some prerequisites. These prerequisites are needed for one of three elements of these sampling techniques – stratification, ratio expansion based on absolute APTL, and ratio expansion based on relative APTL. Because the length of a one-way vehicle run can vary for a given route, the average length of each route for the relative-APTL ratio expansion should be calculated as the ratio of annual total vehicle revenue miles and annual total vehicle revenue one-way trips along that route.

### Table 2. Applicable Modes and Required Data by Sampling Technique

<table>
<thead>
<tr>
<th>Sampling Techniques</th>
<th>Mode</th>
<th>Required Data</th>
</tr>
</thead>
<tbody>
<tr>
<td>Direct simple random sampling (base)</td>
<td>All</td>
<td>- All units operated</td>
</tr>
<tr>
<td>Direct stratified sampling</td>
<td>Other than DR</td>
<td>- All units operated by stratum</td>
</tr>
<tr>
<td>Absolute-APTL simple random sampling</td>
<td>All</td>
<td>- 100% UPT</td>
</tr>
<tr>
<td>Relative-APTL simple random sampling</td>
<td>Fixed-route with 2+ routes</td>
<td>- 100% UPT by route</td>
</tr>
<tr>
<td>Absolute-APTL stratified sampling</td>
<td>Other than DR</td>
<td>- 100% UPT by stratum</td>
</tr>
<tr>
<td>Relative-APTL stratified sampling</td>
<td>Fixed-route with 2+ routes</td>
<td>- 100% UPT by route &amp; stratum</td>
</tr>
<tr>
<td></td>
<td></td>
<td>- Average length of each route</td>
</tr>
</tbody>
</table>

Notes: DR = demand response  
APTL = average passenger trip length  
UPT = unlinked passenger trips

**Expected Relative Efficiency**

Table 1 also summarizes the expected relative efficiency between some of these sampling techniques. Stratification is expected to improve efficiency over simple random sampling for any given estimation method. Otherwise, one would not use stratification because it complicates both data collection and estimation of annual PMT.

Ratio expansion with the absolute-APTL approach is expected to improve efficiency over direction expansion with or without stratification. PMT at any unit of operation (e.g., one-way trips) tends to be proportional to the number of UPT
for that unit. As a result, it is often more efficient to estimate annual PMT as the product of a 100% count of UPT and the absolute APTL from a sample.

Furth (2005) hypothesizes that the relative-APTL approach is more efficient than the absolute-APTL approach. He argues that PMT at any unit of operation tends to be proportional to not only UPT on the unit but also the route length. Since the product of UPT on a unit of operation and the route length is potential PMT for the unit, PMT on a unit of operation tends to be proportional to potential PMT on that unit. As a result, it is expected to be more efficient to estimate annual PMT by multiplying a 100% count of potential PMT and the relative APTL from a sample by each route in a system.

**Methodology**

To analyze the relative efficiency of these six sampling techniques, 83 sample datasets were used that cover 65 agencies and six modes – motorbus, trolleybus, demand-response, vanpool, light rail, and commuter rail with motorbus and trolleybus combined as a single bus mode for analysis.

**Assumptions**

An initial sample size for a given sample dataset to reach the minimum sample size is adjusted for two considerations. One accounts for errors in the sample data. Errors can result from both sampling and non-sampling sources, and these errors may lead to the initial sample size too large or too small for FTA’s requirements. To guard against the latter, a margin of 25% is built into the minimum sample size used in this paper. This margin, however, does not influence the relative efficiency of sampling techniques. The other relates to the minimum size of 10 for each stratum when ratio estimation is used. Bias exists in ratio expansion, and it can become significant when the sample size is below 10 (Furth and McCollom 1987).

The results are presented in relative terms. When comparing the efficiency of Absolute-APTL simple random sampling (40) and direct simple random sampling (200), for example, the result is shown as the percent reduction in minimum sample size by Absolute-APTL simple random sampling from direct simple random sampling \((\frac{40-200}{200} = -80\%)\).

For ease of references, direct simple random sampling sometimes is referred to as the base technique, while the other five techniques as a whole are referred to as non-base sampling techniques. For motorbus services, using the commonly-used
sampling plan in Circular 2710.1A as the base would help transit agencies to determine how much their data collection effort would decline relative to their current effort. Since circular sampling plans are not available for most modes, however, direct simple random sampling is used as the base instead for all modes.

**Data Sources and Characteristics**

Among the 83 sample datasets, 14 are for demand-response, 7 for vanpool, 8 for light rail, 3 for commuter rail, and 51 for bus. According to the Florida Transit Information System, these six modes represent more than 96% of all mode-service type reports submitted to the NTD for 2006. The sample datasets come from two sources. Some are from transit agencies as a result of requests for previous research efforts on sampling for the NTD (Chu and Ubaka 2004, Chu 2006, Chu 2007). Most, however, come from transit agencies in response to a request as part of an effort to develop the *National Transit Database Sampling Manual* (Chu 2009). This later request was sent to each agency that reported to the NTD for 2006 and was for each mode and type of service that each agency reported. For many agencies that sent their sample datasets for multiple years for a given mode and service type, only the latest is used.

The sampling units vary among the sample datasets both across modes and within a mode. For demand-response and vanpool, the sampling unit is always in vehicle days. For bus, it is in round trips for one sample dataset but in one-way trips for all others. For light rail and commuter rail, the sampling unit is in one-way passenger car trips in most cases but is in one-way train trips for a few of the sample datasets. Not separating the results for different sampling units does not affect the relative efficiency between two sampling techniques.

When applicable, stratification is done differently for different modes and sample datasets with information contained in each sample dataset. There are at least issues with post-stratification:

- Information is not always available in a sample dataset for choosing the most useful way. Stratification depends on the type of quantity on which stratification is executed and how stratification is done with a chosen quantity.
- Stratification is not always based on information available before sampling. For vanpool, for example, it is done uniformly across all datasets with two strata defined by the sample median of APTL. For bus, stratification is based on route length if available but is based on APTL otherwise. In real applica-
tions, one should use something that is known before sampling occurs, such as route length, as the basis for stratification.

As a result, the efficiency of stratification-based sampling techniques may not be exact for each applicable sample dataset. This shortcoming may influence the relative efficiency between stratification and simple random sampling. It does not negatively impact the paper’s main purpose—to motivate transit agencies to explore these sampling techniques.

**Actual Relative Efficiency**

This section empirically examines the relative efficiency of the sampling techniques from four perspectives. After describing the analysis method, the results for these perspectives are presented in separate sub-sections:

- Potentials and Variations shows the potentials in efficiency improvements from using the various sampling techniques as well as the variations in how each sampling technique may do for a particular case.
- Effects of Estimation Methods compares empirically the efficiency of the different estimation methods for a given basic sampling method. Comparisons are made separately between Relative-APTL simple random sampling and direct simple random sampling and between the two approaches to ratio expansion.
- Effects of Sampling Methods compares empirically the efficiency of the two basic sampling methods for any given estimation method.
- Ratio Expansion versus Stratification examines their relative efficiency empirically.

**Potentials and Variations**

The potential for each sampling technique to improve efficiency is great and can be shown both for individual sample datasets and for all sample datasets combined. For individual sample datasets, the potential is evidenced by the highest percent reduction for each applicable sampling technique and mode. The potential is shown between direct simple random sampling and each of the other five sampling techniques.

Table 3 shows both minimum and maximum percent reductions in minimum sample size for each non-base sampling technique from the base technique (i.e., direct simple random sampling) by mode. Also shown is the number of sample datasets
used. For Absolute-APTL simple random sampling, for example, the highest reduction ranges from 65% for vanpool and 98% for commuter rail. For the sample datasets as a whole, the potential is equally significant. While not shown separately, the total minimum sample sizes for all sample datasets is 14,341 under Absolute-APTL simple random sampling but 30,687 under the base technique, a reduction of 53%.

**Table 3. Potentials and Variations in Efficiency Improvements**

<table>
<thead>
<tr>
<th>Non-Base Sampling Techniques</th>
<th>Range of Reduction from Base</th>
<th>Modes</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Demand-Response</td>
</tr>
<tr>
<td>Direct Stratified Sampling</td>
<td>Lowest</td>
<td>-26%</td>
</tr>
<tr>
<td></td>
<td>Highest</td>
<td>-38%</td>
</tr>
<tr>
<td></td>
<td># Datasets</td>
<td>7</td>
</tr>
<tr>
<td>Absolute-APTL Simple Random Sampling</td>
<td>Lowest</td>
<td>-28%</td>
</tr>
<tr>
<td>Absolute-APTL Stratified Sampling</td>
<td>Highest</td>
<td>-88%</td>
</tr>
<tr>
<td></td>
<td># Datasets</td>
<td>14</td>
</tr>
<tr>
<td>Absolute-APTL Stratified Sampling</td>
<td>Lowest</td>
<td>-70%</td>
</tr>
<tr>
<td>Relative-APTL Simple Random Sampling</td>
<td>Highest</td>
<td>-90%</td>
</tr>
<tr>
<td></td>
<td># Datasets</td>
<td>7</td>
</tr>
<tr>
<td>Relative-APTL Stratified Sampling</td>
<td>Lowest</td>
<td>-74%</td>
</tr>
<tr>
<td></td>
<td>Highest</td>
<td>-79%</td>
</tr>
<tr>
<td></td>
<td># Datasets</td>
<td>2</td>
</tr>
<tr>
<td>Relative-APTL Stratified Sampling</td>
<td>Lowest</td>
<td>-77%</td>
</tr>
<tr>
<td></td>
<td>Highest</td>
<td>-80%</td>
</tr>
<tr>
<td></td>
<td># Datasets</td>
<td>2</td>
</tr>
</tbody>
</table>

Notes: To show transit agencies the potential of sampling techniques for efficiency improvements and how these improvements vary, this study chose to use the percent reduction from the base technique for each applicable non-base sampling technique. It may be argued that reduction in the number of units is more relevant for saving costs than percent reduction. Percent reduction is found to be easier for presentation.

Understanding the potential for improvement is important, but equally important is to understand the variations. First, Table 3 shows some variation in whether a non-base sampling technique may actually improve efficiency. The lowest reduction being zero by direct stratified sampling for bus shows that stratification alone does not necessarily improve efficiency. In this particular case, routes in the sample dataset are separated into three groups, with 10 and 20 miles as the separation criteria. In addition, the lowest reduction being positive 2% by Absolute-APTL simple random sampling for bus shows that ratio expansion does not always improve
efficiency over direct expansion. Other than these exceptions, however, these non-base sampling techniques improve efficiency from the base technique. More important, Table 3 shows that the degree of improvements depends highly on the mode and the actual operating conditions through comparing the minimum and maximum reductions for each sampling technique and each mode.

What might be the causes of these large variations in efficiency improvements across the different sample datasets for a given sampling technique? The direct cause of these large variations in efficiency improvements is differences in the degree of variation in the relevant parameter across the different sample datasets. The parameter is PMT per unit of sampling for direct expansion, APTL for Absolute-APTL ratio expansion, and relative passenger trip length for Relative-APTL ratio expansion. For example, the Absolute-APTL approach works well when APTL does not vary much from one vehicle trip to another. This often is the case in transit systems in which the routes have roughly the same length, but not when a transit agency has a mix of long-distance express routes and shorter local routes. If an agency’s routes are of varying length without a clear breakpoint, there is some benefit to stratifying; but if the routes can be neatly divided into very long, express routes and similar-length local routes, stratification can be extremely effective in improving sampling efficiency. In terms of any indirect causes that lead to the differences in the degree of variation in the relevant parameter for a given sampling technique, all we know is that they likely reflect a combination of all service characteristics, including the service geography, the route networks and service polices of all modes in the same service geography, the spatial origin and destination patterns for travelers, etc.

Effects of Estimation Methods

The effects of estimation methods can be determined in two steps. The first step determines the effects of Absolute-APTL ratio expansion over the base, and the other determines the effects of the Relative-APTL approach over the Absolute-APTL approach. For each step, the analysis is done both without stratification and with stratification.

Figure 1 shows the effects of Absolute-APTL ratio expansion for each applicable mode and sample dataset, with Figure 1a for the case of without stratification and Figure 1b with stratification:

- Without stratification, Absolute-APTL ratio expansion does not always improve efficiency. The exception is the bus sample dataset where the correlation between UPT and PMT is extremely low at 0.42. Otherwise,
Absolute-APTL ratio expansion improves efficiency over the base technique for all sample datasets. The improvement is uniformly high for light rail and commuter rail, but is more varied for the other modes. Part of the modal difference in the variation of efficiency improvements within a mode is the result of differences in the number of sample datasets used.

- With stratification, Absolute-APTL ratio expansion improves efficiency for all applicable sample datasets, including the bus sample dataset where Absolute-APTL ratio expansion is less efficient without stratification. In addition, the efficiency improvements appear to be far more uniform both within modes and between modes.

**Figure 1a. Absolute-APTL Simple Random versus Base**

**Figure 1b. Absolute-APTL Stratified versus Direct Stratified**
Relative-APTL ratio expansion is applicable to 12 bus sample datasets, 2 light rail datasets, and 1 commuter rail dataset. For the small number of applications to the rail modes, Relative-APTL ratio expansion does not improve efficiency over Absolute-APTL ratio expansion either with or without stratification. For bus, as shown in Table 4, however, their relative efficiency depends on the operating conditions of transit agencies. The 12 sample datasets have been separated into four groups, and the following patterns of relative efficiency are observed:

- The Relative-APTL approach is far more efficient for the first five datasets under both basic sampling methods. Among these cases, the advantage of the relative-APTL approach is far greater under simple random sampling than under stratified sampling.
- The Relative-APTL approach is slightly more efficient for datasets 6-8 under both basic sampling methods.
- The Relative-APTL approach is slightly more efficient for datasets 9-10 under stratified sampling but not under simple random sampling.
- The Absolute-APTL approach is more efficient for datasets 11-12 under both basic sampling methods.

### Table 4. Relative Efficiency of Relative- and Absolute-APTL Approaches for Bus Service

<table>
<thead>
<tr>
<th>Relative Efficiency</th>
<th>Datasets</th>
<th>Base</th>
<th>Absolute-APTL Simple Random</th>
<th>Relative-APTL Simple Random</th>
<th>Absolute-APTL Stratified</th>
<th>Relative-APTL Stratified</th>
</tr>
</thead>
<tbody>
<tr>
<td>Relative-APTL better</td>
<td>1</td>
<td>520</td>
<td>530</td>
<td>218</td>
<td>299</td>
<td>169</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>438</td>
<td>358</td>
<td>160</td>
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<td></td>
<td>3</td>
<td>916</td>
<td>744</td>
<td>457</td>
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<td>4</td>
<td>871</td>
<td>486</td>
<td>180</td>
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<tr>
<td></td>
<td>5</td>
<td>695</td>
<td>414</td>
<td>171</td>
<td>150</td>
<td>103</td>
</tr>
<tr>
<td>Relative-APTL slightly better</td>
<td>6</td>
<td>156</td>
<td>40</td>
<td>27</td>
<td>23</td>
<td>23</td>
</tr>
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<td></td>
<td>7</td>
<td>297</td>
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<td></td>
<td>8</td>
<td>237</td>
<td>38</td>
<td>35</td>
<td>37</td>
<td>32</td>
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<tr>
<td>Relative-APTL slightly better when stratified</td>
<td>9</td>
<td>289</td>
<td>113</td>
<td>133</td>
<td>60</td>
<td>54</td>
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<td>10</td>
<td>690</td>
<td>243</td>
<td>336</td>
<td>108</td>
<td>100</td>
</tr>
<tr>
<td>Absolute-APTL better</td>
<td>11</td>
<td>505</td>
<td>198</td>
<td>218</td>
<td>183</td>
<td>190</td>
</tr>
<tr>
<td></td>
<td>12</td>
<td>348</td>
<td>70</td>
<td>144</td>
<td>70</td>
<td>82</td>
</tr>
</tbody>
</table>
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Effects of Sampling Methods

The effects of stratification versus without stratification can be determined for each estimation method—direct expansion, Absolute-APTL ratio expansion, and Relative-APTL ratio expansion:

- With direct expansion, stratification improves efficiency for all four applicable modes (Figure 2a). The improvement is similar in percentage terms for commuter rail and vanpool, but varies quite significantly across sample datasets for light rail and bus.

- With Absolute-APTL ratio expansion, whether stratification improves efficiency differs significantly across modes (Figure 2b). Stratification improves efficiency at least 50% for all vanpool sample datasets. With two exceptions, it also improves efficiency for bus though the effect varies more across the sample datasets. For light rail and commuter rail, however, stratification makes sampling less efficient. This reversed relative efficiency for stratification does not necessarily reflect the characteristics of stratification, but rather is likely the result of three factors in applying stratification with ratio expansion to these two rail modes. The minimum sample size is small for the two rail modes under Absolute-APTL simple random sampling, at least for the sample datasets available for this paper. For the 8 light rail sample datasets, the minimum sample size under Absolute-APTL simple random sampling is 52 for one sample dataset and under 33 for all other sample datasets. For the 3 commuter rail sample datasets, the minimum sample size under Absolute-APTL simple random sampling is under 40. The second factor is the minimum stratum size of 10 used. The third factor is the number of strata used for stratification.

- With Relative-APTL ratio expansion, stratification improves efficiency for all 20 applicable bus sample datasets (Figure 2c), although with a wide range in the degree of improvements. For the single applicable sample dataset for commuter rail, stratification is less efficient. For the two applicable sample datasets for light rail, stratification is more efficient for one sample dataset but is less efficient for the other.
Figure 2a. Direct Stratified versus Base

Figure 2b. Absolute-APTL Stratified versus Absolute-APTL Simple Random
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Figure 2c. Relative-APTL Stratified versus Relative-APTL Simple Random

Ratio Expansion versus Stratification

With one exception for vanpool, Absolute-APTL simple random sampling is far more efficient than direct stratified sampling for all sample datasets from vanpool, light rail, and commuter rail (Figure 3a). The relative efficiency between ratio expansion and stratification, however, is mixed for bus. For the cases where the minimum sample size is toward the lower end of the full range, Absolute-APTL simple random sampling is still more efficient than direct stratified sampling. For the cases where the minimum sample size is toward the higher end of the full range, however, the opposite appears to be the case. This pattern can be observed in Figure 3b, which shows the minimum sample size for these two sampling techniques in an x-y plot, with the two axes on the same scale along with a 45-degree diagonal line for easy comparison.
Figure 3a. Percent Reductions for Four Mode

Figure 3b. Minimum Sample Size for Bus

Conclusions
This paper has examined the minimum sample size required by each of six sampling techniques for estimating annual passenger miles traveled to meet Federal Transit Administration’s 95% confidence and 10% precision levels for the National Transit Database. The six sampling techniques and the findings about them are relevant to any method of data collection for estimating annual passenger miles traveled through random sampling. The findings have important implications for both transit agencies and consultants as practitioners and for researchers.
For practitioners, the potential cost savings from using these sampling techniques is great, both for individual cases and for the transit industry as a whole. Practitioners should be motivated by these great potentials to consider these sampling techniques. But the actual cost savings for any specific case depends highly on the mode, the operating conditions, and the sampling technique. Practitioners should explore the actual cost savings possible for each sampling technique for their particular mode and operating conditions before deciding whether any of these sampling techniques should be used and which of them should be used.

For researchers, the paper provides the most comprehensive picture of how six modern sampling techniques may perform across a wide range of modes and operating conditions. This comprehensive picture shows that the expected improvement in sampling efficiency for certain sampling techniques can be significantly greater or significantly less than what researchers have expected from both theoretical considerations and prior limited empirical evidence. For example, estimating passenger miles traveled through ratio expansion on the basis of Relative-APTL has been hypothesized and shown with data from one agency to be more efficient than ratio expansion based on Absolute-APTL (Furth 2005). The results from 12 bus samples, 2 light rail samples, and one commuter rail sample in this paper, however, show that the relative efficiency of these two approaches also vary by mode and the operating conditions of individual cases.

Acknowledgments

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